Statistical approach to assess radon-222 long-range atmospheric transport modelling and its associated gamma dose rate peaks

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Abstract. There is a need for a validation framework for long-range atmospheric transport modelling dedicated to radionuclides. For distances greater than 50 km, the modelling of radionuclide deposition and ambient gamma dose rate evaluation are particularly difficult to validate, since it has been mainly only observed after the accidents of Chernobyl and Fukushima. There is however a natural wet deposition phenomenon leading to numerous well-observed gamma dose rate events: the scavenging of radon-222 progeny by rain. Radon-222 exhalation from the soil to the atmosphere, its decay, its progeny, its own transport, the transport of its progeny, their deposition, and the consequent ambient gamma dose rate are then modelled at the European scale. This whole atmospheric radon model from soil (exhalation) to soil (deposition) needs to be validated by comparison with observations.

The biggest benefit of this case study is the number of events that serve as a comparison. For a statistical evaluation of the performance of the model, we compared its results with gamma dose rate observations over a period of two years, gathering more than 15 000 peaks greater than 10 nSv h−1 above the background radiation. Two sets of metrics were used to assess the agreement between the model and observations: on a case by case basis (peak to peak) and continuously (whole time series of gamma dose rates and air concentrations). Particular attention was paid to defining the metrics in order to remove the background radiation level and to exclude outlier stations.

We found that 48 % of the gamma dose rate peaks are well modelled, a fraction of which can rise up to 89 % by being more tolerant with the success criteria. The model has proven to be of the correct magnitude, with room for substantial improvement. Overall, the modelling shows better recall than precision: i.e. a tendency to produce more false positives than false negatives. It is also less effective in reproducing the highest peaks. Exhalation, vertical mixing and deposition have been identified as the three main features which could improve this model.

Now validated, with all its limitations, the atmospheric radon model may serve for its primary purpose, the validation of atmospheric transport modelling and its input data. It also may serve as a framework to test any exhalation model on a national or continental scale. Moreover, it is useful to learn how to properly use the data of an ambient gamma dose rate network, and how to compare this data to modelled data. Finally, some interesting features concerning the assessment of outdoor concentrations of radon-222 became apparent.

1 Introduction

Atmospheric transport modelling (ATM) dedicated to radionuclides is challenging to validate with regard to the few events studied – apart from accidental releases such as Chernobyl or Fukushima. Here, we are particularly interested in the validation of the long-range (> 50 km) ATM of IRSN, known as LdX (Groëll et al., 2014). This model has been used for more than a decade for the long-range atmospheric transport of radionuclides, e.g. to evaluate the consequences of the Fukushima Daiichi nuclear power plant accident (Mathieu et al., 2012; Sato et al., 2020; Quérel et al., 2021) or for Comprehensive Nuclear-Test-Ban Treaty Organization (CTBTO) challenges (Eslinger et al., 2016; Maurer et al., 2018). More details are given in Sect. 2.1. To validate...
LdX, we focused on radionuclides of natural origin, among which radon-222 and its progeny. These radionuclides indeed provide thousands of observed gamma dose rate peaks per year measured by Télérây, the IRSN national and early warning monitoring network (Télérây, 2022). A radon plume stays in the atmosphere for up to one week, travels across several hundreds of kilometres (Arnold et al., 2010; Barbosa et al., 2017), making the use of a long-range ATM such as LdX relevant. Long-range ATM validation has already been done with radon-222 air concentration (Jacob et al., 1997; Zahorowski et al., 2004; Karstens et al., 2020; Zhang et al., 2021), but not necessarily with gamma-dose rate evaluation or from a statistical point of view (Inomata et al., 2007).

The physics behind the observed gamma dose rate peaks due to radon and its progeny requires knowledge of geology and pedology for radon exhalation, nuclear physics for radioactive decay and progeny, and atmospheric physics—including transport, wet and dry depositions—for peak occurrence. Geology and pedology are characterised by fields that do not usually feed the ATM dedicated to radionuclides, whereas nuclear and atmospheric physics modelling are common between this radon-dedicated study and any other releases of radionuclides into the atmosphere. In other words, modelling gamma dose rate peaks due to radon progeny is a new way to validate the tools used to model the consequences of a nuclear release into the environment.

This study describes the current modelling of the gamma dose rate due to atmospheric radon and its progeny. The statistical performances of the modelling in reproducing the Télérây network measurements are described. Statistical strengths and weaknesses of the modelling are then shown. This allows for a comprehensive view of the ATM validity domain, thus identifying critical features which could be improved.

1.1 Radon-222 exhalation

Radon-222 is a noble gas naturally emitted by rocks containing uranium-238. The surface exhalation flux is mainly driven by the rock composition, but it is also influenced—to different degrees—by both rock and soil porosity, permeability, humidity and temperature, as well as water table depth, geological faults or atmospheric pressure (Griffiths et al., 2010; Manohar et al., 2013; Karstens et al., 2015).

Correct modelling of all these effects needs complete input data for all these parameters—in space and time, as well as a complete, independently validated model. For this study, the temporal fluctuation of the radon exhalation is simplified to a monthly variation. Section 4 will statistically show the necessity of at least taking this monthly variation into account. The exhalation map is based on the work of Karstens et al. (2015). Since this exhalation map does not include data after 2013, we consider the monthly exhalation as the mean of the corresponding month over a 7 year period from 2006 to 2012. Over France, an IRSN exhalation map is used instead (Ielsch et al., 2017). Note that the IRSN source term represents the maximum exhalation rate and so is corrected monthly by the Karstens et al. (2015) monthly variation covering the same territories. It is also important to note that radon-222 sea exhalation is neglected, considering it is several thousand times smaller than continental exhalation. The exhalation in August and January are illustrated in Fig. 1.

1.2 Radon and its progeny in the atmosphere

Once emitted into the atmosphere, radon is quickly transported like any other gas or aerosol particle. As a noble gas, it is unreactive and poorly soluble. Radon is consequently not subject to dry and wet depositions (Fujinami, 1996; Mercier et al., 2009; Paatero et al., 2012; Bottardi et al., 2020). It is transported without depletion other than its radioactive decay. Its half-life of 3.8 days allows radon-222 to travel across several hundred kilometres within the atmosphere.

The successive radon-222 progeny have a half-life shorter than 30 minutes to lead-210, the half-life of which is 22 years. See Fig. 2 for the series of short-lived radon progeny. Unlike radon-222, the progeny are not noble gases, and quickly bind to aerosol particles. These radionuclides are all considered in the particulate form in this study. They are therefore subject to deposition processes, among which wet scavenging is the most efficient to lead to large deposits on the ground, up to several kBq m$^{-2}$.

Among the short-lived progeny of radon, lead-214 and bismuth-214 are significant gamma emitters (Fig. 2), the radiation intensity of which could be measured in terms of ambient gamma dose rate. The deposition of these two progeny can raise the ambient gamma dose rate up to 100 nSv h$^{-1}$ above the natural background radiation—generally in a range between 50 and 100 nSv h$^{-1}$ in France. The increase generally lasts between five and 30 minutes, depending on the rain and the radon air concentration. Because of the short half-lives of lead-214 and bismuth-214, these deposited radionuclides disintegrate within several hours, leading to a gamma dose rate decrease. A rapid increase followed by a decrease together form a gamma dose rate peak. In total, a peak usually lasts 2 to 5 hours.

To sum up, radon and its progeny are radionuclides transported over long distances in the atmosphere and the wet deposition of some of them is often measured, therefore suitable as a case study.

2 Method

The objective was to validate the ATM dedicated to radionuclides and also to identify its possible improvements. To do so, the exhalation, the atmospheric transport and the deposition of radon-222 and its short-lived progeny were modelled, as well the ambient gamma dose rate they caused. The
method described here is a way to model this phenomenon and a way to compare it to observations.

2.1 Model settings

All simulations were run with LdX, the operational long-range atmospheric transport model used by IRSN for nuclear emergencies, included in the IRSN’s C3X operational platform (Tombette, 2014). This Eulerian model is derived from the Polair3D model (Mallet and Sportisse, 2004) of the Polyphemus platform (Mallet et al., 2007; Quélo et al., 2007), which is designed to study regional-scale air quality issues. Decay modes and products have been added afterwards.

LdX is an off-line model. Meteorological data of the numerical weather prediction (NWP) ARPEGE of Météo-France is used. This data is projected into the LdX domain of computation, which covers western and central Europe. The domain is displayed in Fig. 3. The ARPEGE horizontal resolution of 0.1° is kept, leading to a horizontal mesh of 321 × 201 cells. A vertical resolution of 14 levels is used, with the first level from 0 to 40 m a.g.l. (above ground level), and the 14th level between 6600 and 8800 m a.g.l. ARPEGE data is provided with an hourly frequency, and LdX uses an internal time step of 10 min in order to better capture temporal variations.

The precipitation data from the NWP is substituted by radar observations, in order to improve the space time resolution of the wet deposition processes. Radar data is also provided by Météo-France and have a raw spatial resolution of 1 km and a temporal resolution of 5 min. Radar data is projected onto the LdX domain resolutions of 0.1° and 10 min. Rainfall intensities are thresholded at 0.1 mm·h⁻¹, considering that a smaller rainfall level is not relevant (Wang et al., 2016).

Vertical diffusion of Louis (1979) is used above the atmospheric boundary layer (ABL) and in the ABL for stable conditions. Troen and Mahrt (1986) is used for the ABL in unstable conditions.

The dry deposition velocity is set at 2 mm·s⁻¹. The below-cloud scavenging and in-cloud scavenging used are described in Table 1, with Λ the scavenging coefficient (s⁻¹) and I the
Table 1. Wet deposition schemes (Quérel et al., 2021).

<table>
<thead>
<tr>
<th></th>
<th>Scavenging coefficient (s⁻¹)</th>
</tr>
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<tbody>
<tr>
<td>Below-cloud</td>
<td>( \Lambda = 5 \times 10^{-5} )</td>
</tr>
</tbody>
</table>
| In-cloud       | \( \Lambda = 5 \times 10^{-4} f^{0.64} \)

rainfall intensity (mm). These coefficients are justified in Quérel et al. (2021). They are effective in a cloud, defined with the Cloud Fraction given by ARPEGE. A Cloud Fraction threshold value of 0.1 is arbitrary set to define the cloud presence. Cloud base height cannot be lower than 3000 m. In the event of absence of a cloud diagnosed above the rain, a by-default cloud at 500–5000 m is used.

ICRP-38 data is used for the half-lives and decay products (ICRP, 1983). The ambient gamma dose rate at ground level is computed as the sum of the radiations due to the concentration and the deposit, using the dose coefficients of the FGR 12 (Eckerman and Ryman, 1993).

Finally, a two year computation with these settings lasts about one month of computation time on a single processor. The modelled period runs from 1 January 2020 to 31 December 2021, inclusive.

2.2 Observations

The ambient gamma dose rates used for this study come from the Téléray monitoring network. In 2021, it consisted of 439 ambient gamma dose rate monitoring stations spread over France, recording data every 10 min all year round. 8346 and 8116 peaks higher than 10 nSv h⁻¹ above background were measured in 2020 and 2021 in France. These large numbers allow a statistical approach to validate an ATM but, like any other observation data set, must be well understood for a relevant comparison with model results.

2.2.1 Téléray network observations

Created in 1991, the IRSN’s Téléray network covers ambient radioactivity stations spread all over France (Téléray, 2022), with clusters around each nuclear facility (Fig. 4). The purpose of this network is to quickly detect any unusual rise in ambient radioactivity, in the event of a nuclear accident in France or abroad. Téléray stations, sensitive to gamma radiation, provide a measurement of the ambient gamma dose equivalent rate expressed in nSv h⁻¹.

Data is provided every 10 min, but we use an hourly arithmetic mean. This temporal degradation is done because gamma counts are more reliable spread over a 1 h period, avoiding recording errors and being less noisy. In addition, here, only the rain data have a 10 min resolution. All the other met data have a 1 h resolution. Thus, the 1 h aggregation corresponds to the worst input data resolution.

2.2.2 Background radiation subtraction

The natural ambient gamma dose rate is composed of potassium-40 and three natural chains: thorium-232 (via thallium-208 progeny), uranium-238 (via its bismuth-214 progeny) and uranium-235 gamma emission. Cosmic rays can also be added as a component of the natural gamma dose rate, depending on the station altitude (Bossow et al., 2017). The background radiation in France is generally between 50 and 100 nSv h⁻¹. This variability is due to the bedrock nature, the soil composition and the depth profiles of the radionuclides in the soil (Saito et al., 2012; Melintescu et al., 2018). In this study, the increase in the gamma dose rate due to the radon air concentration and deposition is independent of this background radiation.

The background radiation depends on the soil composition, its water content, the soil occupancy and the altitude. It is consequently different for each station and it evolves over time. The airborne radon part of the gamma dose rate can only be observed with a correct subtraction of the background radiation. There are two ways of doing this. The first way is to model this background radiation and the second is to mathematically determine it from the measured gamma dose rate time series. The first method is difficult and still uncertain, considering the poor knowledge of the soil composition surrounding each station.

It is for this reason that the background radiation is subtracted using a Gaussian filter. Gaussian filters are commonly used in signal processing. A background time series is computed for each station using the ndimage module of the scipy Python’s library (https://docs.scipy.org/doc/scipy/reference/ndimage.html, last access: 21 July 2022; Virtanen et al., 2020). A sigma of 100 h is set for the computation. This value allows for any presence of radon peaks in the background time series, while keeping a fast computing analysis. The background time series is then subtracted from the measured one, providing an observation time series without its background component. This time series could finally be compared to the simulated gamma dose rate. Figure 5 gives an example of a background radiation subtraction.

2.3 Observations-model comparison

A gamma dose rate peak is defined as a temporary elevation of the dose rate. A peak is defined by a location (that of the measurement station), a time (the moment of the maximum) and a peak intensity (the maximum gamma dose rate level once the background radiation has been subtracted). Two peak value levels are used here: peaks > 10 nSv h⁻¹ and peaks > 50 nSv h⁻¹. These two levels were chosen to acquire the largest number of peaks in order to obtain good statistics and to work on the model’s ability to reproduce the highest peaks, i.e. the ones that trigger a radiological alert on the monitoring network.
2.3.1 Definitions of failures and successes

For each observed gamma dose rate peak, simulation success or failure were evaluated. Three categories were used: true positive (TP), false negative (FN) and false positive (FP). A TP is a peak observed that is well simulated. A FN is a peak observed but not simulated. A FP is a peak simulated but not observed.

A simulated peak is never perfectly identical to an observed peak. There is thus a necessity to define the tolerance to consider that a simulated peak is similar to an observed one. A tolerance in intensity, in time and in space can be set. A tolerance in intensity is relative to the dose rate value reached by the observed and the simulated peak. A factor 2 is used in this study. A factor 5 would lead to very good scores but would be poorly sensitive to the model setting and so this would prevent the identification of sources of improvement. Conversely, an intensity tolerance of a factor 1.1 leads to only 8% of TP. The factor 2 in intensity is thus a balanced factor between severity and complacency, making it possible to effectively measure the impact of a parameter on the quality of the modelling. In addition, it should be recalled that the observations are themselves error accompanied (standard deviation $\sim 2.5 \text{nSv h}^{-1}$), and errors are added by the background radiation subtraction. Figure 6 illustrates a series of five peaks greater than 10 nSv h$^{-1}$, counted as TP with a fac-
tor 2 tolerance. Concerning the time tolerance, an offset of 1 h is allowed between the timing of the observed and simulated local maximum. For the year 2021, 73% of the simulated peaks were in time accordance with the observed peaks to the nearest hour. A 1 h tolerance is therefore strict enough for these study purposes. Note that the timing offset between simulated and observed peaks is zero-centred (Fig. 7), meaning there is no systematic error of the peak timing. Concerning spatial tolerance, despite the improvements and its positive impact on the statistics, none is set in the study; the gamma dose rate value simulated in the grid cell containing the Téléray station is used. Indeed, a one-cell tolerance was tested – selecting the best value of the 9-cells around the station. There are 83% of the observed peaks simulated within a factor 2 using this spatial tolerance, but considering that rainfall events measured by radar are well located, it is difficult to justify this spatial tolerance without in-depth studies.

Figure 5. Example of background radiation subtraction. In black, the observed gamma dose rate. (a) Raw data. (b) Data after background radiation subtraction. (In red, simulated values.)

Figure 6. Five TP in a row, at the Soultz–Haut–Rhin station at the start of summer 2021. TP are marked with black arrows.

Figure 7. Histogram of the timing offset between observed and simulated peaks for the year 2021.
Statistics can be compiled by counting the number of TP, FN and FP over several time periods. It is difficult to compare results integrated over a year to those integrated over a month, or over two months, which is why we also used a statistical common way to aggregate TP, FN and FP, using the recall and precision metrics, themselves aggregates in the $F_1$ score. The recall is the fraction of TP compared to the total number of observed peaks (Eq. 1). The precision is the fraction of the TP compared to the total number of simulated peaks (Eq. 2). The $F_1$ score is the harmonic mean of the recall and the precision (Eq. 3).

\[
\text{recall} = \frac{TP}{TP + FN} \quad (1)
\]
\[
\text{precision} = \frac{TP}{TP + FP} \quad (2)
\]
\[
F_1 \text{ score} = 2 \frac{\text{recall} \times \text{precision}}{\text{recall} + \text{precision}} \quad (3)
\]

In addition to these three metrics dedicated to the peaks, there is a need to measure the performance of the whole simulated gamma dose rate time series compared to the observed ones. The goal is to detect systematic bias or strong decorrelation between them. To do so, Pearson correlation coefficient (PCC), Factor 2 (FAC2) and Wasserstein distance are used. The PCC measures the linear correlation between the observed ($\mu^{ob}$) and the simulated gamma dose rate time series ($\mu^{sim}$). This value is between $-1$ and $1$, and the agreement increases as the value approaches $1$. The FAC2 is described in Eq. (4), evaluating the fraction of simulated values including in a factor 2 of the observed ones at the same time. The Wasserstein distance is computed with the Wasserstein function of the stats module of the SciPy Python package (https://docs.scipy.org/doc/scipy/reference/stats.html, last access: 21 July 2022; Virtanen et al., 2020). The closer the Wasserstein distance is to zero, the closer are the observed and simulated time series.

\[
\text{FAC2} = \frac{1}{N_t} N \left( \frac{1}{2} \mu^{ob}_t \leq \mu^{sim}_t \leq 2 \mu^{ob}_t \right) \quad (4)
\]

The next step is to clean up the observation dataset. Some observations indeed appear not relevant for the comparison with the simulation. The metrics described above are applied to each station and the ones for which the scores are the worst are studied in detail. If a station produces bad metrics for reasons related to an observational bias or default, this station is tagged as an outlier and it is then excluded from the observation database.

A station could be an outlier for different reasons: a large gap in data, a drift in observation due to a calibration error, a station in a mountainous area, or the presence of anthropic gamma dose rate peaks, for instance due to some industrial activities occurring in its neighbourhood. The three global metrics (PCC, FAC2 and Wasserstein distance) are particularly useful to detect these outliers. The first results are a presentation of the outliers found in this two-year study.

### 3 Results: statistical performance of the model

#### 3.1 Identified outliers

The worst recalls were obtained for stations located at high altitude. For example, the Pic-du-Midi-de-Bigorre station, located at 2876 m a.s.l. (above sea level), gave 85 FN over the 2020–2021 period, including six gamma dose rate peaks greater than $50 \text{nSv h}^{-1}$. Figure 8a shows four of them observed between June and July 2020. Figure 8b is zoomed around the peak of the 30th June. These FN could be explained in two ways: average value assessment and snow deposition. LdX is dedicated to assessing an average concentration in a cell (as a reminder, about $10 \times 10 \text{km}$), and does not represent variability within the cell. This is also true for the underlying meteorological model, and especially the modelled topography is considerably smoothed and the mean altitude in the grid-cell is much lower than the contained summits. This has to be kept in mind when performing model-to-measurement comparisons in mountainous areas where large wind variabilities and major vertical transport and mixing processes are induced by the sub-grid topography in reality but missed by the model (Rotach et al., 2014, 2015). High altitude stations are finally more subject to snowfall. Particle scavenging by snow is however not yet well modelled in LdX. In addition to the Pic-du-Midi-de-Bigorre station, Aiguille-du-Midi lies in the same outlier category. These two stations give a recall of $19\%$ (Aiguille-du-Midi) and $11\%$ (Pic-du-Midi-de-Bigorre) over the 2020–2021 period. This is three to six time lower than the $62\%$ obtain in mean for the validated stations (see Sect. 3.2).

Conversely, some stations lead to a large number of FP. One of these stations, the Tour Eiffel station, appears to be located too high above the ground (100 m a.g.l., Fig. 9a and b) to be sufficiently sensitive to gamma rays emitted from ground deposition.

The stations with a lot of missing data have a particularly poor Wasserstein distance. The worst score in 2021 was obtained by the Lumbres station with a value of 0.42, with an obvious lack of data after April 2021 (Fig. 10). It appears that all stations with a Wasserstein distance greater than 0.1 have at least three months of missing observations. There are thus 21 identified outlier stations for the year 2020 and 19 for the year 2021. Note that 7 stations are excluded for both years (Fumay, Grenoble-GN, Lyon, Montpellier, Ruoms, St-Paul-Trois-Chateaux and Sully-sur-Loire).

The FAC2 illustrates the cases where observations are obviously underestimated. The worst FAC2 of 2021 is obtained...
at the Rodez station with a value of 0.7% (see Fig. 11a and b time series). It appears that, at this station, the observed values are never greater than 3.3 nSv h⁻¹. Four more stations are excluded due to a too low FAC2 in 2020 and 2021: Rodez, Vincennes, Paris-Sacré-Cœur and Cruas-SIT. The common feature of these four stations is an obstructed horizon (shielding effect), explaining the strong differences between the observed and modelled gamma dose rate peaks. These are categorised as “stations with incompatible horizon”, as well as the Paris-Tour-Eiffel station. This evaluation is indeed based on dose rate coefficients assuming a flat, uniformly contaminated plain, without any obstacles.

The PCC outliers do not bring any other outliers. A high number of FN can also be a clue to exclude some stations. With 8 FN in 2020 for peaks greater than 50 nSv h⁻¹, La-Seyne-sur-Mer is the worst of this metric (see Fig. 12a and b time series), while the second one has only 3 FN. These gamma dose rate peaks are in fact due to anthropic gamma shots. This station outlier is thus excluded. In the same way, Omonville-la-Petite has a large number of FN, in fact gamma dose rate peaks due to industrial activities. The Freiburg station also gives a large number of FN, which are linked to snow deposition. Aerosol particle scavenging by snowfall events are not yet specifically simulated in our ATM. Since out of the domain of validity of the ATM, this station is also excluded.

In total, 31 outlier stations were excluded in 2020 and 29 in 2021. The summary of these outliers is provided in Table 2, giving a total number of 395 stations in 2020 and 393 stations in 2021.

### 3.2 Statistics for 2020 and 2021

Once the outliers were identified and excluded from the measurement database used to compare with the simulations, statistics were compiled over the whole period of simulation, from 1 January 2020 to 31 December 2021 on the remaining stations. Table 3 summarises the impact of the removal of outlier stations. It appears that the removal impact is limited,
Figure 10. Observed and simulated ambient gamma dose rates at the Lumbres station in 2021.

Figure 11. Observed and simulated ambient gamma dose rates at the Rodez station. (a) In June and July 2021. (b) The 24 June 2021.

Table 2. Summary of the outlier stations.

<table>
<thead>
<tr>
<th>Outlier type</th>
<th>Rules</th>
<th>Number of excluded stations for 2020</th>
<th>Number of excluded stations for 2021</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stations in mountainous areas</td>
<td>Recall &lt; 20 %</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Stations with an incompatible horizon</td>
<td>FAC2 &gt; 5 %</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Stations with not enough data</td>
<td>Dist. Wasserstein &gt; 0.1</td>
<td>21</td>
<td>19</td>
</tr>
<tr>
<td>Stations with anthropic peaks</td>
<td>More than 50 FN</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Stations implying unmodelled physics</td>
<td>More than 50 FN</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>31</td>
<td>29</td>
</tr>
</tbody>
</table>
Figure 12. Observed and simulated ambient gamma dose rates at the La-Seyne-sur-Mer station. (a) In May and June 2020. (b) The 9 June 2020.

Table 3. Statistics for peaks greater than 10 nSv h\(^{-1}\) during the period 2020–2021 with and without the outlier stations.

<table>
<thead>
<tr>
<th>Metrics</th>
<th>2020–2021 without outliers</th>
<th>2020–2021 outliers included</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of observed peaks</td>
<td>15 761</td>
<td>16 783</td>
</tr>
<tr>
<td>Recall</td>
<td>62 %</td>
<td>60 %</td>
</tr>
<tr>
<td>Precision</td>
<td>39 %</td>
<td>37 %</td>
</tr>
<tr>
<td>(F_1) score</td>
<td>48 %</td>
<td>46 %</td>
</tr>
</tbody>
</table>

The statistics are more relevant for peaks greater than 10 nSv h\(^{-1}\), due to a larger number of events. Peaks greater than 50 nSv h\(^{-1}\) are rare, with only 90 observed events (263 simulated). The higher the peaks, the worse the results (Table 4). Recall is 20 % less for peaks greater than 50 nSv h\(^{-1}\) than the 10 nSv h\(^{-1}\) peaks, meaning that fewer observed peaks are indeed simulated, relatively speaking. It is worst with the precision, with a 25 % decrease of the metrics, meaning that only a fraction of the simulated peaks greater than 50 nSv h\(^{-1}\) are indeed observed. The \(F_1\) score confirms these results. If this trend turns out to be statistically confirmed, it will be difficult to understand why it is more difficult to simulate the higher gamma dose rate peaks. The wet deposition schemes or precipitation issues could be a possible explanation, and would need further study.

2020 and 2021 have similar statistics for peaks greater than 10 nSv h\(^{-1}\), with less than 6 % difference for the recall, precision (Table 5). Recall is better for 2021 than 2020, whereas precision is better for 2020 than 2021. The same behaviour is observed for peaks greater than 50 nSv h\(^{-1}\), with greater differences: recall 10 % better in 2021, and precision 10 % worse.

The number of observed peaks cannot be seen as homogeneous on a monthly basis (Fig. 13a). There is a maximum of peaks in June and September, and a minimum during the first three months of the year. Winter months are indeed known to have a smaller exhalation rate, due to soil humidity and freezing (López-Coto et al., 2013; Karstens et al., 2015), unlike summer months, where exhalation is maximum. During the months of July and August there are less rainfall events than in June and September, leading finally to a smaller number of events in July and August. This monthly variation is well reproduced by the modelling (Fig. 13b). The number of FP is then not month-dependent.

Like the monthly shape, there is also an hourly shape. Figure 14a illustrates the time of day at which FN occur for the whole period 2020–2021, with a first maximum of FN between 06:00 and 07:00 UTC and a second between 18:00 and 19:00 UTC. This feature is not observed on the TP and on the FP. It can be noticed that this pattern is intensified for the month of July and August (Fig. 14b). The morning peaks are not related to rainfall events. It appears that they are due to night inversion (stratification of the lower layers of the atmosphere). This diurnal phenomenon has already been well observed for radon air concentration activity (Arnold et al.,
Table 5. Statistics for peaks greater than 10 and 50 nSv h\(^{-1}\) for 2020 and 2021, without the outliers.

<table>
<thead>
<tr>
<th>Metric</th>
<th>&gt; 10 nSv h(^{-1}) in 2020</th>
<th>&gt; 10 nSv h(^{-1}) in 2021</th>
<th>&gt; 50 nSv h(^{-1}) in 2020</th>
<th>&gt; 50 nSv h(^{-1}) in 2021</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of observed peaks</td>
<td>8005</td>
<td>7756</td>
<td>62</td>
<td>28</td>
</tr>
<tr>
<td>Recall</td>
<td>59 %</td>
<td>65 %</td>
<td>40 %</td>
<td>50 %</td>
</tr>
<tr>
<td>Precision</td>
<td>41 %</td>
<td>37 %</td>
<td>20 %</td>
<td>10 %</td>
</tr>
<tr>
<td>(F_1) score</td>
<td>49 %</td>
<td>47 %</td>
<td>27 %</td>
<td>17 %</td>
</tr>
</tbody>
</table>

Figure 13. Monthly distribution of the peaks for the period 2020–2021. (a) Observed peaks. (b) Simulated peaks.

Figure 14. Hourly distribution of FN. (a) For the period 2020–2021. (b) For July and August 2020 and 2021.

2009; Barbosa et al., 2017) and ambient gamma dose rates (Melintescu et al., 2018). During the night, the soil is indeed colder than the air, cutting convection due to warming of the lower atmosphere layer caused by the soil, and vertical mixing is then limited during the night. Radon exhalation is exactly the same during the day or night, so the radon exhaled at night accumulates in the first layer of the atmosphere (0–40 m a.g.l. in our modelling). Due to this radon accumulation, its progeny are also in greater concentrations, leading to a gamma dose rate increase. At sunrise, the soil warms up again and convection restarts shortly after, leading to a vertical mixing of the atmosphere, decreasing the radon concentrations and the ambient gamma dose rate in the lower layers. This rise and decrease in the gamma dose rate can be interpreted as a gamma dose rate peak. The example of Limoges during the last two weeks of July 2020 is relevant to this point (Fig. 15a and b), where observed gamma dose rate amplitudes may exceed 20 nSv h\(^{-1}\). Most of these observed peaks are FN, probably meaning that the nightly vertical mixing is probably overestimated by the vertical diffusion schemes used by LdX. This atmospheric phenomenon is especially important during summer, which explains the high number of FN during this period. A part of the late afternoon peaks are correlated to rainfall events, possibly due to thunderstorms breaking out in summer at this time of the day. Further studies will be necessary to confirm this hypothesis.

4 Discussion

The results obtained from the modelling of atmospheric transport and deposition of radon and its progeny provide some reassuring certainties about the ATM capability and the entire modelling chain. Yet, it also raises questions and sets out a path for improving the radon modelling chain, from exhalation to the gamma dose rate.
4.1 Certainties

This comparison between an ATM dedicated to radionuclide transport and ambient gamma dose rate measurements was here conducted in “peace time”, testing all the elements of the domestic operational chain and would also be carried out in the event of a nuclear accident leading to atmospheric releases. Several aspects of this particular modelling-observation comparison have been assessed and can be transposed from one case to another. One is the identification of outlier stations. Respectively 29 and 31 stations were identified for 2020 and 2021 as not comparable with this modelling. In a hypothetical emergency with a release of radionuclides into the atmosphere, these stations should be considered by-default as out of the domain of validity of this kind of modelling.

Another gained certainty concerns the timing of the simulated results. Validation of gamma dose rates evaluated from LdX results was previously done following the Fukushima incident (Saunier et al., 2013), but the radon modelling chain presented here allows validation against thousands of events using ARPEGE NWP data coupled with rain radar observations. On this basis we have now gained confidence in the model to statistically simulate the gamma dose rate due to a deposition event at the right time.

The results appear to be consistent over the two years studied. The same behaviour was observed in failures and successes throughout this period. It is a key point for the reliability of the model and the observations. Without being perfect, it must be noted that the modelled peak intensities are of the same magnitude as the observed peak intensities. A $F_1$ score of 82% with a tolerance of factor 5 in the peak intensity – 89% if a spatial tolerance on the peak location and a 3 h temporal tolerance is added – indicates that the simulated peaks intensities are consistent with the observed intensities. Even for high-intensity peaks (greater than 50 nSv h$^{-1}$), we obtained a $F_1$ score of 80% with tolerances. The solution for the background subtraction is then validated, and the modelling seems to be immune to a major systematic error.

Concerning exhalation, we have presented only one model herein, the combination of an IRSN term over France and the Karstens et al. (2015) one over the rest of Europe. We also performed a sensitivity test on these exhalation maps, using a 100% Karstens et al. (2015) exhalation and constant-in-time exhalation. It showed a relative independence on the exhalation map choice (Table 6), with a recall, precision and $F_1$ score equal within a 3% range. However, using a constant-in-time source leads to a score degradation, notably for the precision, due to a greater number of FP. Note that the time dependency of the exhalation rate is more critical in winter, with 2380 FP in January–February 2021 without monthly variations, compared to only 912 FP during the same period with a monthly variation. These results were expected, as the constant-in-time exhalation is set for the summer months. The impact of the exhalation map deserves a more complete and dedicated study (see next section). However, we can already affirm that a monthly variation of the exhalation rate is mandatory for atmospheric radon modelling.

Finally, a list of gamma dose rate peak modelling failures has already been understood, in addition to the already de-
scribed outlier stations. Errors can also be caused by poorly modelled atmospheric phenomena, such as atmosphere stability during summer nights. This leads us to be careful with the model results obtained in such circumstances, further studies dedicated to resolve this issue are needed. It is however as important to know the domain of validity of a modelling, especially for an ATM used to help manage the consequences of a potential nuclear accident.

4.2 Future developments

This study attests to already substantial work, with appreciable lessons, but further developments have been identified. With a model of atmospheric radon, from exhalation to ambient gamma dose rate, and with the appropriate metrics, it is now possible to statistically and locally measure the impact of model improvements of exhalation, meteorology, atmospheric transport, deposition and gamma dose rate estimation.

An expected major improvement concerns the exhalation of radon. We have here used monthly variations deduced from the 2006–2012 period studied by Karstens et al. (2015). To start, we have to set our radon exhalation rate to the hourly soil water content, and possibly to other parameters such as the atmospheric pressure, the water table depth and the, soil porosity. The results of the RadoNorm (grant agreement No. 900009 – Euratom Research and Training Programme 2019–2020) and TraceRADON (Röttger et al., 2021) European projects should be helpful for this. In addition, a more complete sensitivity study to the exhalation map could be performed. This could be the opportunity to test other exhalation maps, such as those of Szegváry (2007) and López-Coto et al. (2013).

Another major further development concerns atmospheric vertical mixing, proved as poorly modelled during various late night periods. In a Eulerian ATM like LdX, vertical mixing is modelled by vertical advection (given by the NWP), and by vertical diffusion (also called \(K_z\)). Vertical diffusion schemes are particularly difficult to validate. Atmospheric radon appears as an opportunity to work on this item, for instance thanks to the ICOS network (Heiskanen et al., 2021; Grossi et al., 2020). Some stations of this European network provide radon-222 air concentrations for several heights above ground level. It is an opportunity to validate the vertical mixing modelling in the spirit of the Vargas et al. (2015) works, or, at least, to specify the domain of validity of the actual vertical diffusion schemes. Improvements in radon-222 air concentration measurements are also an opportunity to validate the native output data of the ATM (Grossi et al., 2020), unaffected by deposition, contrary to the progeny. Note that this radon air concentration data can also be used to validate the exhalation rate maps.

Deposition modelling, particularly wet deposition, could also benefit from further developments. We have to understand why the actual model seems less efficient in reproducing gamma dose rate peaks with the highest intensities, greater than 50 nSv h\(^{-1}\) than the smaller ones. We suspect an issue with the rainfall rates and/or the wet deposition scheme. Radar observation native resolution (1 km) are indeed degraded to fit to the other meteorological data resolution (0.1°, \(\sim 10\) km). In thunderstorm conditions, rainfall rates are high with strong spatial gradients, both averaged by spatial interpolation. There is then a possibility of a deposition to be evaluated with incorrect inputs. Concerning deposition schemes, we use here a very simple scheme, only depending on the rainfall intensity (see Table 1 in Sect. 2.1). However, in fact, the scavenging coefficient depends on the particle size distribution (Quérel et al., 2014), and other difficult to assess parameters such as electric charges (Lemaître et al., 2020). The wet deposition scheme used here is possibly neither adapted to the particle size distribution of the attached-to-particles radon progeny, nor to their physical and chemical properties. After the Fukushima case (Leadbetter et al., 2015; Quérel et al., 2021), atmospheric radon could be a good case study to evaluate wet deposition sensitivity, including in long-range atmospheric transport modelling. The other key point could be the implementation of scavenging by snow. It is known that the vast majority of the rainfall events at European latitudes start as snow before melting to rain, so it therefore must be important to distinguish below-cloud scavenging by rain and snow (Leadbetter et al., 2015). In addition to this, a hundred snow deposition events were identified for the winter 2020–2021 on the Téléray network, which could be used as a specific validation set.

Other topics can be explored in the future concerning atmospheric radon modelling: the station surroundings and their impact on the ability of the model to reproduce the observation or the sensitivity of the NWP choice.

5 Conclusions

In conclusion, a comprehensive modelling of atmospheric radon-222 and its progeny has been set up. Radon exhalation, transport through the atmosphere, decay, progeny, progeny deposition and ambient gamma dose rate evaluation were performed in order to model the gamma dose rate peaks observed by a radiation monitoring network. We were particularly interested in the gamma dose rate peaks due to scavenging by rain of the radon-222 progeny, which are to aerosol particles. The primary purpose of this study was to add validation cases for LdX, the operational atmospheric transport modelling used by IRSN to evaluate the consequences of a radionuclides release for distances greater than 50 km. The atmospheric radon modelling also reveals itself to be an interesting tool to validate radon exhalation maps and to deal with observations-model comparisons of ambient gamma dose rates.

The two year period 2020–2021 was modelled at the European scale, with a comparison made on Téléray, the radiation network.
monitoring network operated by IRSN (+430 stations). Once the outlier stations were eliminated, 15,761 gamma dose rate peaks greater than 10 nSv h\(^{-1}\) were observed on the network during this period – 90 greater than 50 nSv h\(^{-1}\), which allows better statistics than any past accidental nuclear release. A \(F_1\) score of 48% was obtained on peak detection, with a tolerance of a factor 2 on peak value and 1 h on timing. We observed a model tendency to create more false positives (peak simulated but not observed) than false negatives (peak observed but not simulated). This can be explained by an overestimation of the radon flux, rainfall intensities or wet deposition. Further studies will be needed to improve the modelling. Nevertheless, a \(F_1\) score of 89% is obtained by relaxing the intensity, timing and spatial tolerances, meaning that the atmospheric radon model is definitely at the right magnitude to evaluate gamma dose rate peaks.

Even if the model is at the correct magnitude, there is plenty of room to improve it. Our main objectives will be to use properly parametrised exhalation rates, using soil water content instead of a pre-evaluated monthly variation. Results of the European project RadoNorm and TraceRadon could be the next steps for this topic. Another important objective is to work on the vertical mixing of the atmospheric transport modelling, which appears in this study to be inappropriate for some meteorological situations, for example during stable summer nights. The third main objective is to work on the modelling of gamma dose rates due to scavenging of radon progeny by rain and snow. Scavenging by rain schemes could be improved and validated following this study. Furthermore, scavenging by snow should be implemented and validated, as almost all the precipitation events at European latitudes start as snow before melting to form rain.

Code availability. Codes are not available until their legal status has been clarified. IRSN is working on an open access platform, currently closed.

Data availability. Meteorological data is given at https://donneespubliques.meteofrance.fr/ (Météo France, 2022). Other data is available upon request to the author. As for the code availability,

Author contributions. AQ and DQ contributed to writing – original draft preparation. KM, TD and SC contributed to writing – review and editing. KM contributed to formal analysis. AQ, KM and DQ contributed to methodology, software and validation. DQ, TD and SC contributed to resources. AQ, KM, DQ, TD and SC contributes to visualization. The CRediT contributor roles taxonomy has been used to define author contribution.

Competing interests. The contact author has declared that none of the authors has any competing interests.
A. Quérel et al.: Statistical approach to assess radon-222 long-range atmospheric transport modelling


